Table I. Summary of experimental data.
$\mathrm{nc})]$.
compressional
$\left.\left.\left(e+\delta_{1}\right)\right]\right\}$,

1].
d shear stress
$\left.\frac{\left.\delta_{2}\right)}{\left.1-\delta_{2}\right)}\right]$,
e
$\left.s \delta_{2}\right\}$.
igital computer $t$ compressional y elastic wave parent velocity ratios relating alues of $u_{1}$ are until Eq. (11) equired in the $10 \%$ less than ree-surface ap-
this experiment wo-dimensional off the optic ure 4 illustrates off-axis impact

## RGET

$\left.\begin{array}{ccccc}\hline \hline \begin{array}{c}\text { Distance from } \\ \text { impact } \\ (\mathrm{mm})\end{array} & \begin{array}{c}\text { Shock } \\ \text { velocity } \\ (\mathrm{mm} / \mu \mathrm{sec})\end{array} & \begin{array}{c}\text { Pastic shock } \\ \text { velocity } \\ (\mathrm{mm} / \mu \mathrm{sec})\end{array} & \begin{array}{c}\text { Ramp } \\ \text { Pelocity } \\ (\mathrm{mm} / \mu \mathrm{sec})\end{array} & \begin{array}{c}\text { Shock } \\ \text { velocity } \\ (\mathrm{mm} / \mu \mathrm{sec})\end{array}\end{array} \begin{array}{c}\text { Particle } \\ \text { velocity } \\ (\mathrm{mm} / \mu \mathrm{sec})\end{array}\right]$
and a shock wave breakout that occurs at a local attitude angle $\theta$ with the slit projection at the target.
The optical details are omitted for clarity. One objective lens focuses the slit plane onto the film, hence the slit and film planes are shown as coincident. The polished surface is within the field depth of the other objective lens focusing the grid onto the slit plane, hence the camera slit and grid are shown on opposite sides of the polished target with sets of ray paths as parallel lines. The surface is turned at the breakout and is represented by a rotation vector $\boldsymbol{\alpha}$, parallel to the breakout line, and a unit vector $\mathbf{k}$, perpendicular


Fig. 5. Photograph of an optical lever record. The two-step shock front shows the elastic shock wave followed by the main shock wave. Lines which show no deflection are camera rewrite indicating a permanent deformation of the target.
to the target surface. The shock breakout line moves across the target with an apparent shock velocity $U_{\text {app }}$.

Let $x, y, z$ be a rectangular coordinate axis such that $x$ lies along the slit, and $z$ is directed along the optic axis. Each deflected ray is rotated $2 \boldsymbol{\alpha}$. The displacement of a ray at the grid plane is

$$
2 \alpha \times \mathbf{r}=\left|\begin{array}{ccc}
\mathbf{i} & \mathbf{j} & \mathbf{k}  \tag{17}\\
2 \boldsymbol{\alpha}_{x} & 2 \boldsymbol{\alpha}_{y} & 0 \\
0 & 0 & d
\end{array}\right|=2 d \alpha_{y} \mathrm{i}-2 d \boldsymbol{\alpha}_{x} \mathrm{j}
$$

It is apparent that this relation is similar to the relation

$$
\begin{equation*}
\alpha=a / 2 d \tag{18}
\end{equation*}
$$

described by Fowles, Duvall and Fowles, and by Ahrens and Gregson. Thus the deflection related to turning angle is

$$
\begin{equation*}
\alpha=a / 2 d \cos \theta \tag{19}
\end{equation*}
$$

and can be used to correct Eqs. (2) and (11) through the appropriate free surface relations for the effect of an off-axis impact. The shock breakout rate along the slit is $U_{\text {npp }} \cdot \cos \theta$.

## B. Results

Figure 5 is an optical lever record obtained by hypervelocity impact of a $2.54-\mathrm{cm}$-thick target of 2020-T4 aluminum. The projectile was a steel ball 0.636 cm in diameter and struck the target at a velocity of $5.28 \pm 0.11 \mathrm{~mm} / \mu \mathrm{sec}$. The elastic shock wave followed by the decaying main shock wave is clearly evident. Table I lists values of measured shock and particle velocity.

